



# Modeling and Measurement of Toroidal Currents in the HSX Stellarator

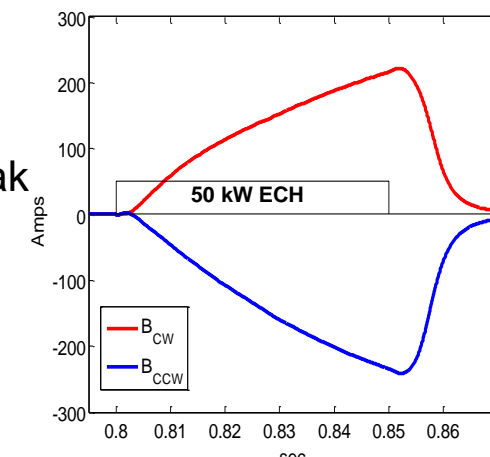


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## Overview

- The Helically Symmetric eXperiment
  - Quasi-Helically Symmetric and almost no toroidal curvature
  - $B_0 = 1$  Tesla
  - 26 kW – 100 kW ECR Heating (1<sup>st</sup> Harmonic)
    - Perpendicular launch
    - Little to no current drive seen during 1 Tesla campaign

- Pfirsch-Schlüter current rotates with the  $|B|$  contours with toroidal angle and is reduced by a factor of 1/3 compared to a conventional stellarator



- Bootstrap current
  - Is in the opposite direction and reduced compared to a tokamak
  - Reduces the rotational transform in HSX
  - Reverses with B-field direction
  - Induces toroidal current with long decay times:  $\tau_{n_i} \mu_0 \geq \tau_{EXP}$

- Evolving current profile is modeled by a diffusion equation with a 3d susceptance matrix

- V3FIT<sup>1</sup> calculations of magnetic signals are compared to diagnostic signals
  - Special thanks to Steve Knowlton, Jim Hanson, and the V3FIT team

## Evolution of Toroidal Current

3d susceptance matrix links toroidal and poloidal currents and magnetic fluxes<sup>2</sup>

$$\mu_0 \begin{pmatrix} I \\ F \end{pmatrix} = \begin{pmatrix} S_{11} & S_{12} \\ S_{21} & S_{22} \end{pmatrix} \begin{pmatrix} \Psi' \\ \Phi' \end{pmatrix} \quad \begin{matrix} S_{12} = S_{21} = 0 \text{ for Tokamaks} \\ S_{11} \approx S_{12} \approx S_{21} \text{ for HSX} \end{matrix}$$

1-D diffusion equation for rotational transform

$$s = \Phi / \Phi_a \quad \frac{dt}{ds} = \frac{1}{\Phi_a^2} \frac{d}{ds} \left( \eta_{\parallel} V' \left[ \frac{\langle B^2 \rangle}{\mu_0} \frac{d}{ds} (S_{11}t + S_{12}) + p' (S_{11}t + S_{12}) - \langle J_{Ni} \cdot B \rangle \right] \right)$$

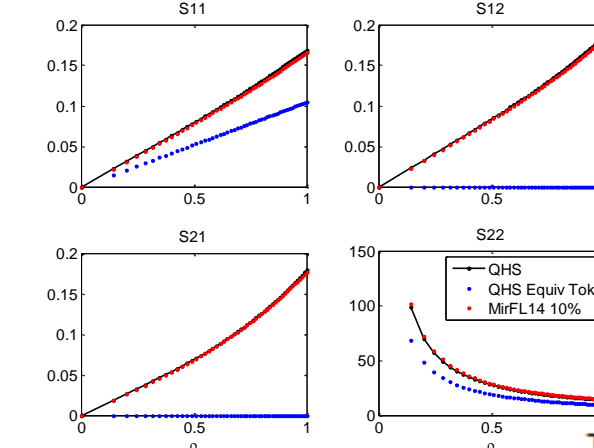
Boundary conditions

On axis: finite current density @ LCFS :set by measurement

Any non-inductive source

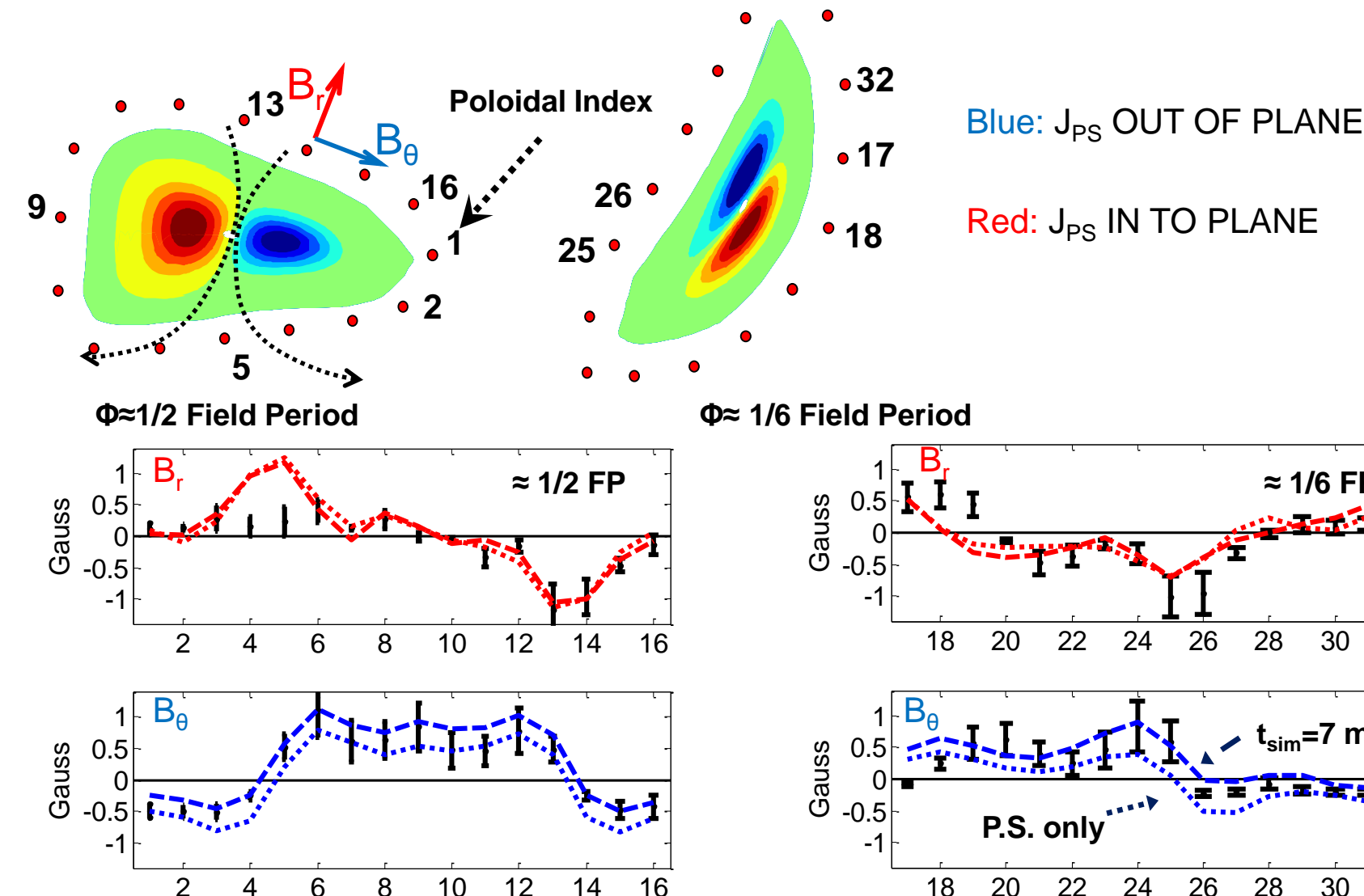
$$\left. \frac{dt}{ds} \right|_{s=0} = 0$$

$$t_{s=1} = \left( \frac{\mu_0 I}{S_{11} \Phi'} - \frac{S_{12}}{S_{11}} \right)_{s=1}$$

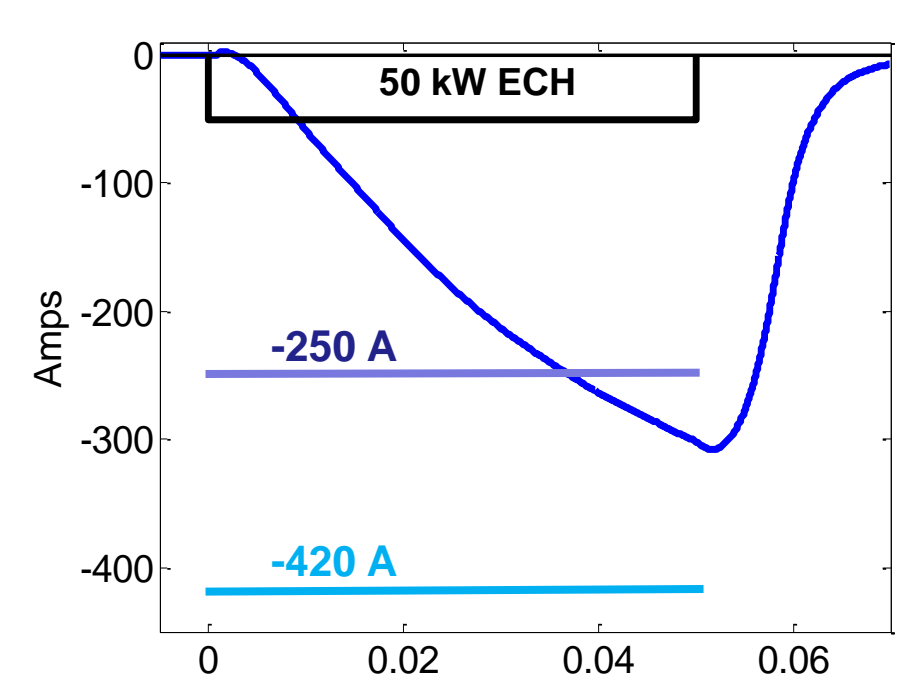
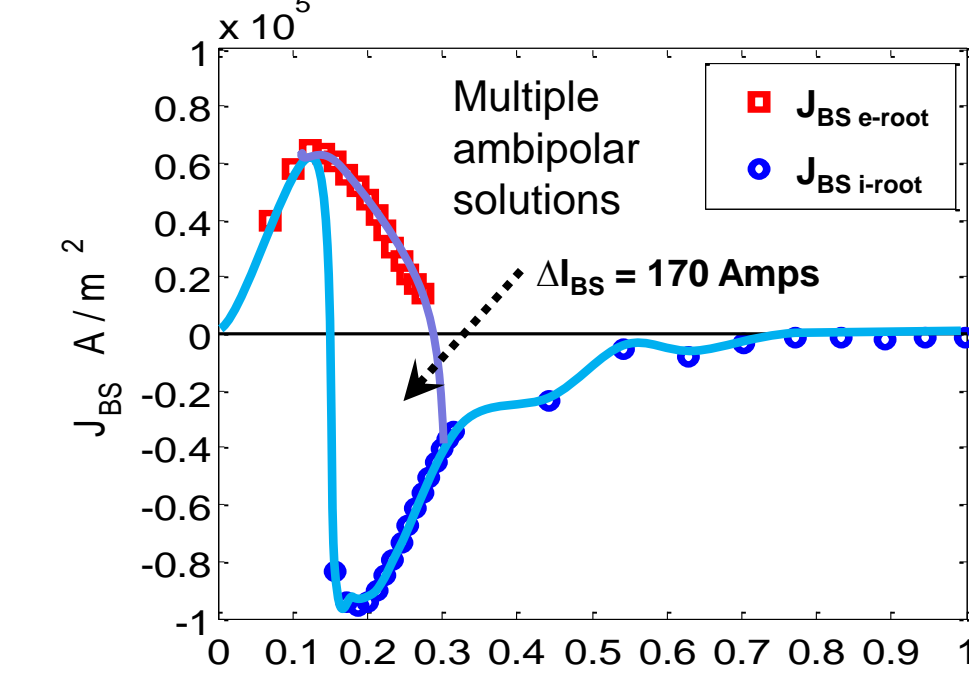
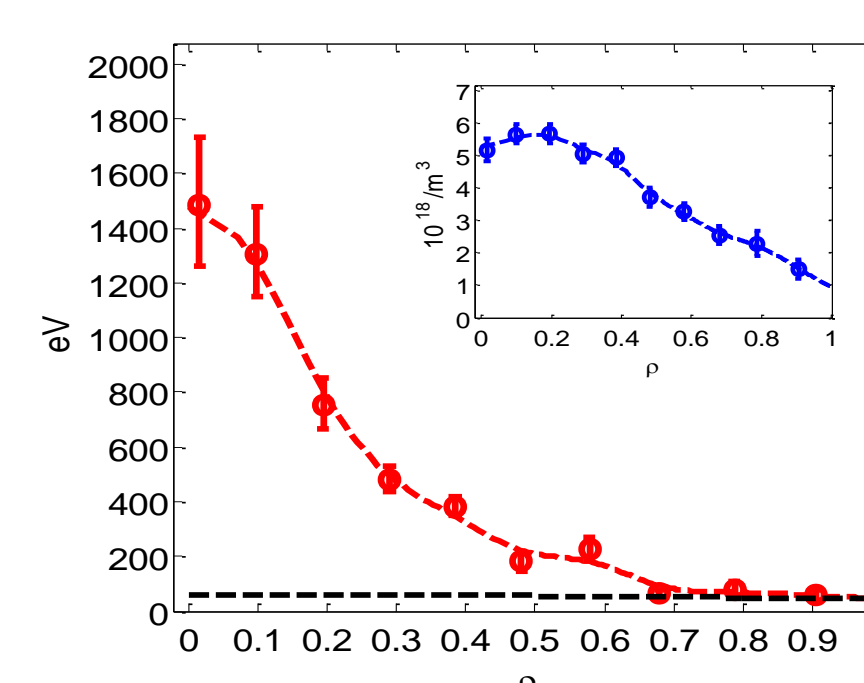


## Pfirsch-Schlüter Current Rotates Helically

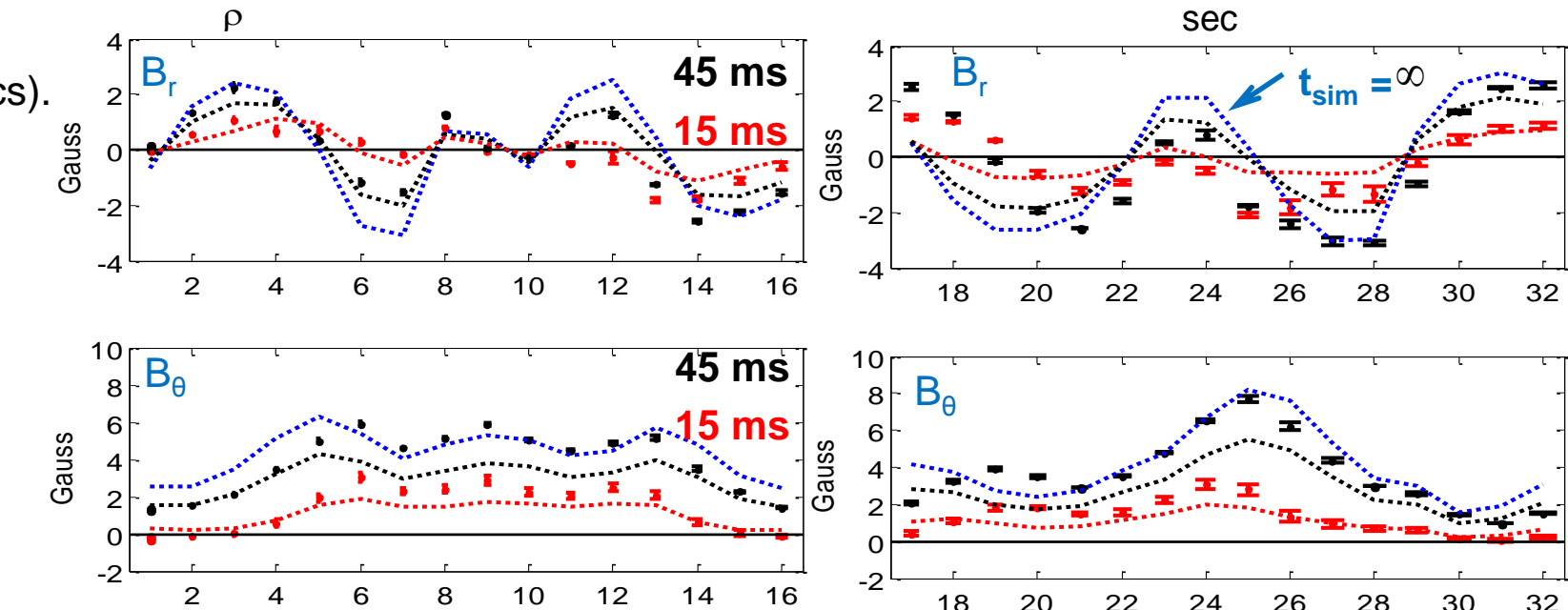
- Pfirsch-Schlüter current exhibits dipole behavior and rotates with  $|B|$  contours
- Sign of signals at two toroidal locations demonstrate a phase shift showing the helical rotation.
- Toroidal curvature is effectively eliminated in HSX



## Bootstrap Current

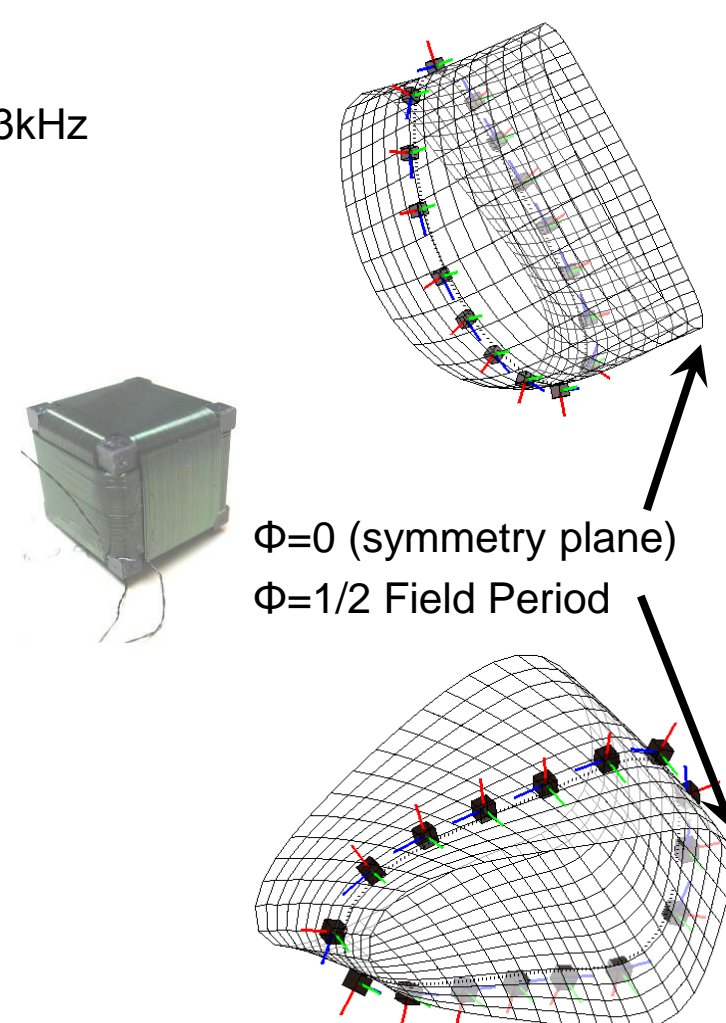


- Te, Ne from Thomson Scattering.
- Ti from ChERS.  $Z_{eff} \approx 1$  from Bremsstrahlung radiation (ChERS optics).
- PENTA<sup>3</sup> calculates the fluxes.  $E_r$  is determined by ambipolarity.
- The electron-root reverses the direction of the bootstrap current
- $B_\theta$  has large unidirectional contribution from  $\langle J \cdot B \rangle$
- $B_r$  is dominated by the  $m=2$  structure of the vacuum vessel
- Measurement evolves slightly faster than simulated values
- Possible sources of error:  $Z_{eff}$ , initial plasma profiles, neoclassical calculation of bootstrap current



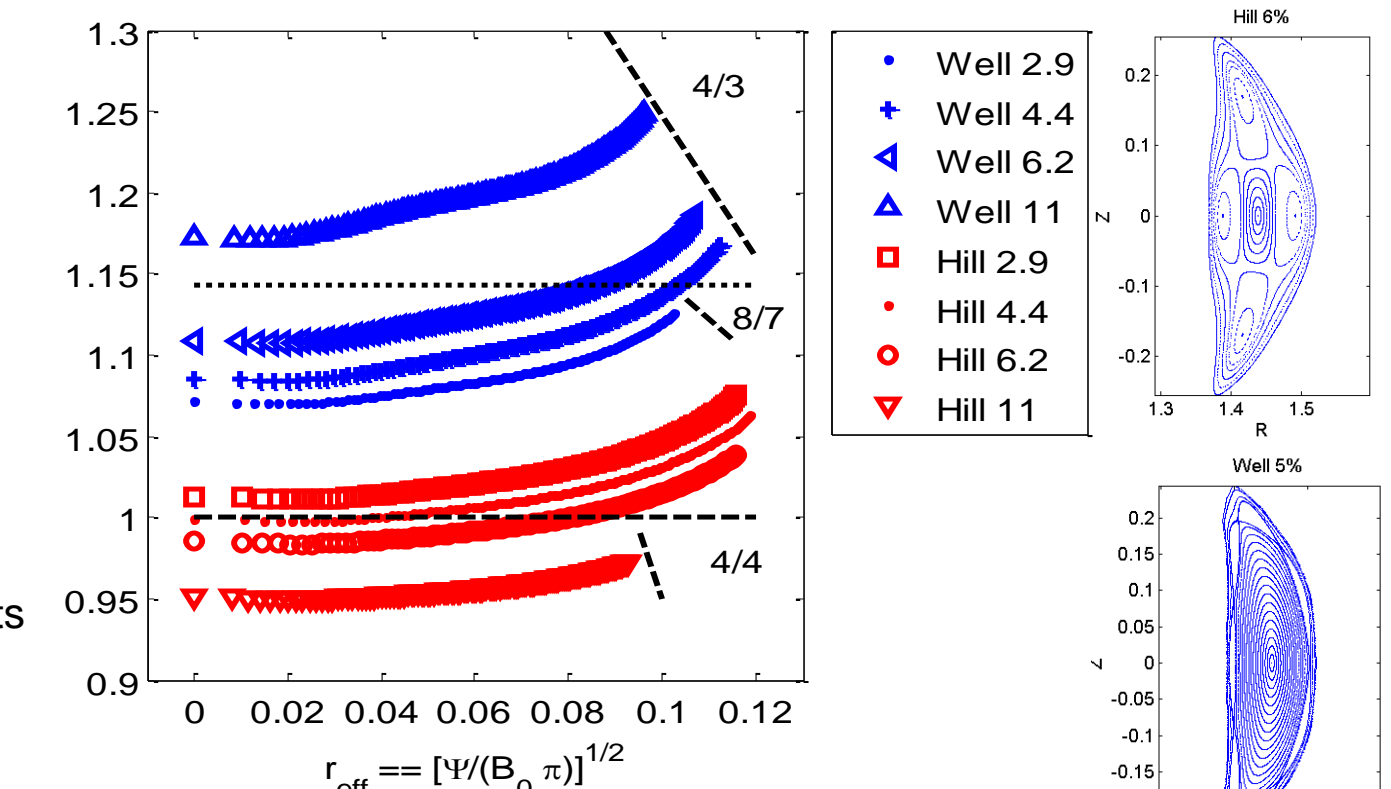
## Diagnostic System

- 2x Rogowski coils ( $I_{tor}$ )
  - External -- Low-frequency response  $\leq 3$ kHz
  - Internal -- High-frequency  $\leq 200$ kHz
- 2x Diamagnetic Loops ( $W_{kin}$ )
  - Internal – High-frequency  $\leq 125$ kHz
- 2x dB/dt triplet array – 32 external triplets
  - MHD and bootstrap currents
  - Low-frequency response
- High-frequency Mirnov array inside vessel
  - 36 coils: 26 poloidal, 10 toroidal
  - Frequency response  $\leq 200$ kHz
- ChERS Diagnostic
  - $T_i$  and  $Z_{eff}$  estimate
- 10-chord Thomson Scattering
  - $T_e(\rho)$  and  $n_e(\rho)$  profiles



## Summary + Future Plans

- The direction of the bootstrap current is reversed and reduced by  $\sim 1/3$  compared to an equivalent tokamak. This results in a reduction in rotational transform.
- Evolving current profile is modeled by a diffusion equation with a 3d susceptance matrix.
- The Pfirsch-Schlüter current rotates with  $|B|$  contours and is reduced by  $\sim 1/3$  compared to a tokamak, demonstrating the lack of toroidal curvature.
- V3FIT for equilibrium reconstruction of HSX plasmas.
- HSX can alter the magnetic spectrum with a set of auxiliary coils
  - Mirror: The helical symmetry is spoiled by introducing  $(n,m) = (4,0)$  component (and harmonics) into magnetic spectrum, affecting equilibrium, bootstrap currents
  - Well/Hill: Rotational transform profile may be raised/lowered, adjusting the location of rational surfaces, vacuum islands



<sup>1</sup> J.D. Hanson, et al, Nucl. Fusion 49 (2009) 075031.  
<sup>2</sup> P. I. Strand and W. A. Houlberg, Phys. Plasmas 8, 2782 (2001).  
<sup>3</sup> D.A. Spong, Phys. Plasmas 12, 056114 (2005).